

# Fluid Mechanics - MTF053

## Lecture 10

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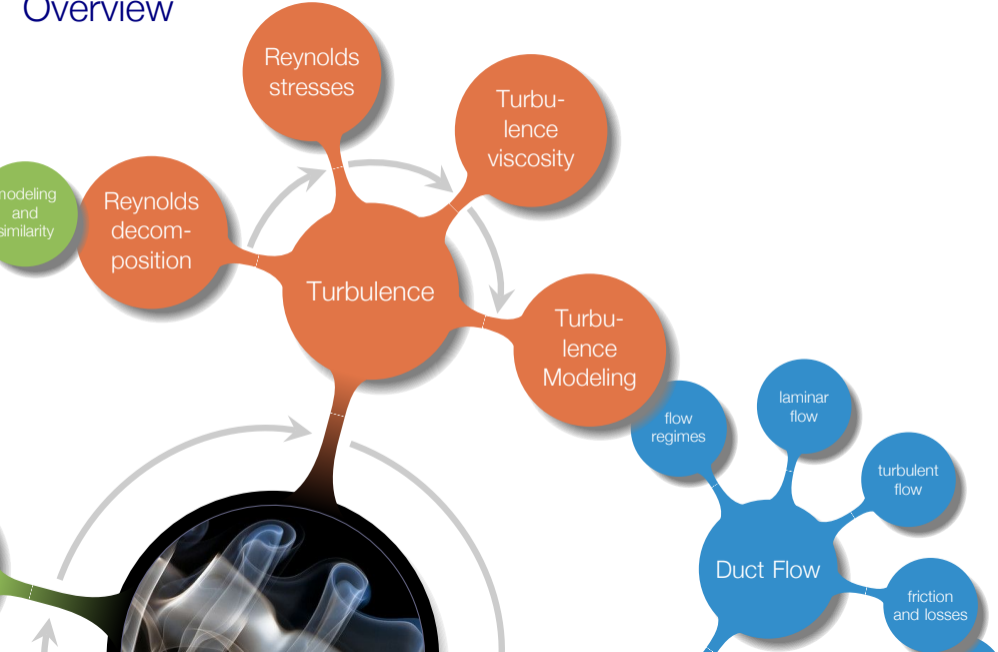
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## Chapter 6 - Viscous Flow in Ducts

# Overview

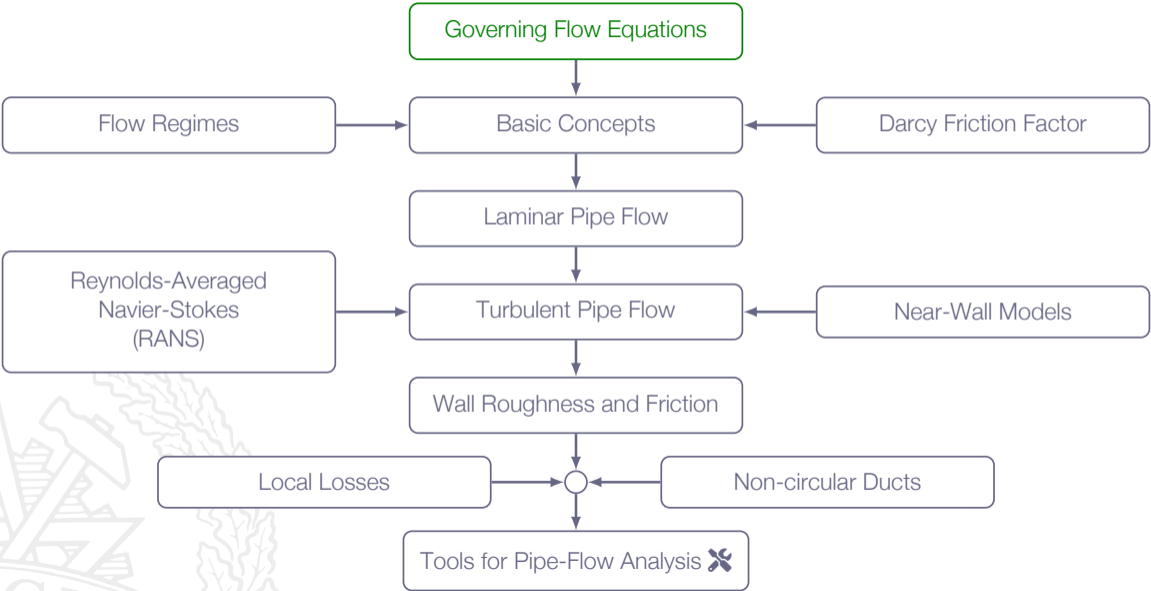


# Learning Outcomes

- 3 **Define** the Reynolds number
- 4 Be **able to categorize** a flow and **have knowledge about** how to select applicable methods for the analysis of a specific flow based on category
- 6 **Explain** what a boundary layer is and when/where/why it appears
- 8 **Understand** and be able to **explain** the concept shear stress
- 18 **Explain** losses appearing in pipe flows
- 19 **Explain** the difference between laminar and turbulent pipe flow
- 20 **Solve** pipe flow problems using Moody charts
- 24 **Explain** what is characteristic for a turbulent flow
- 25 **Explain** Reynolds decomposition and derive the RANS equations
- 26 **Understand** and **explain** the Boussinesq assumption and turbulent viscosity
- 27 **Explain** the difference between the regions in a boundary layer and what is characteristic for each of the regions (viscous sub layer, buffer region, log region)

*if you think about it, pipe flows are everywhere (a pipe flow is not a flow of pipes)*

# Roadmap - Viscous Flow in Ducts



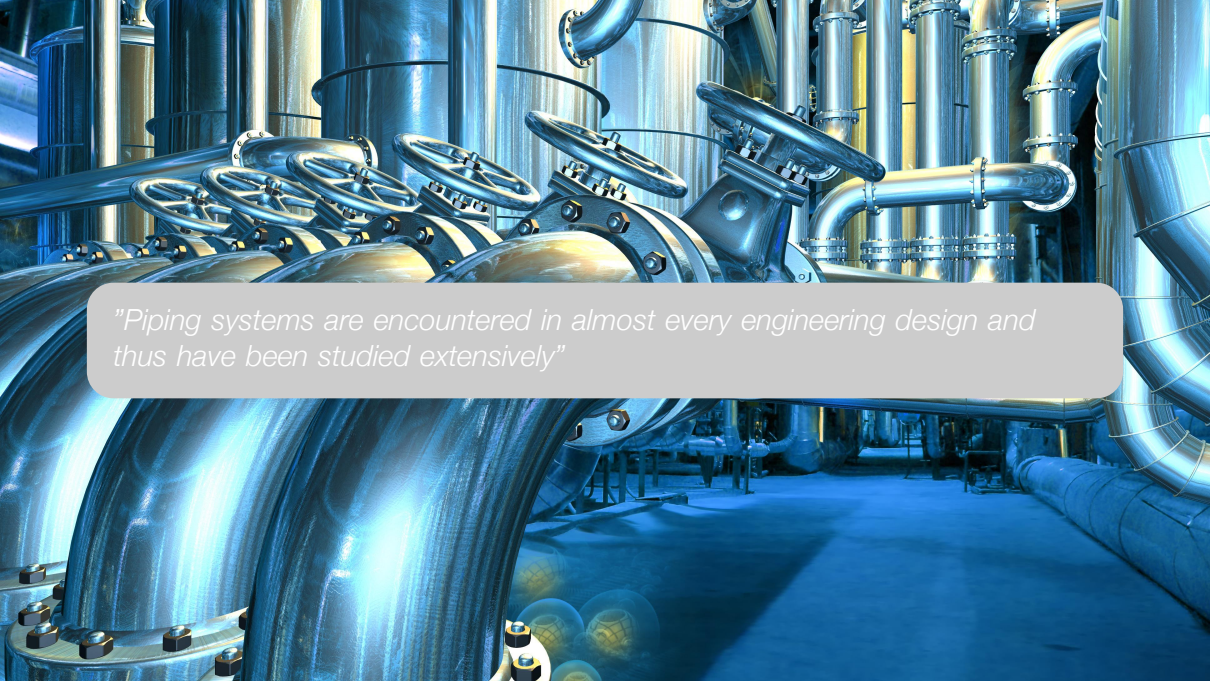
# Complementary Course Material

These lecture notes covers chapter 6 in the course book and additional course material that you can find in the following documents

MTF053\_Equation-for-Boundary-Layer-Flows.pdf

MTF053\_Turbulence.pdf





*"Piping systems are encountered in almost every engineering design and thus have been studied extensively"*

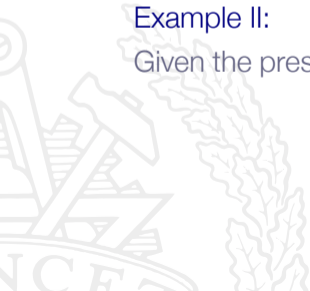
# Typical Pipe-Flow Problems

## Example I:

Given pipe geometry, fluid properties, flow rate, and locations of valves, bends, diffusers etc - estimate the pressure drop needed to drive the flow

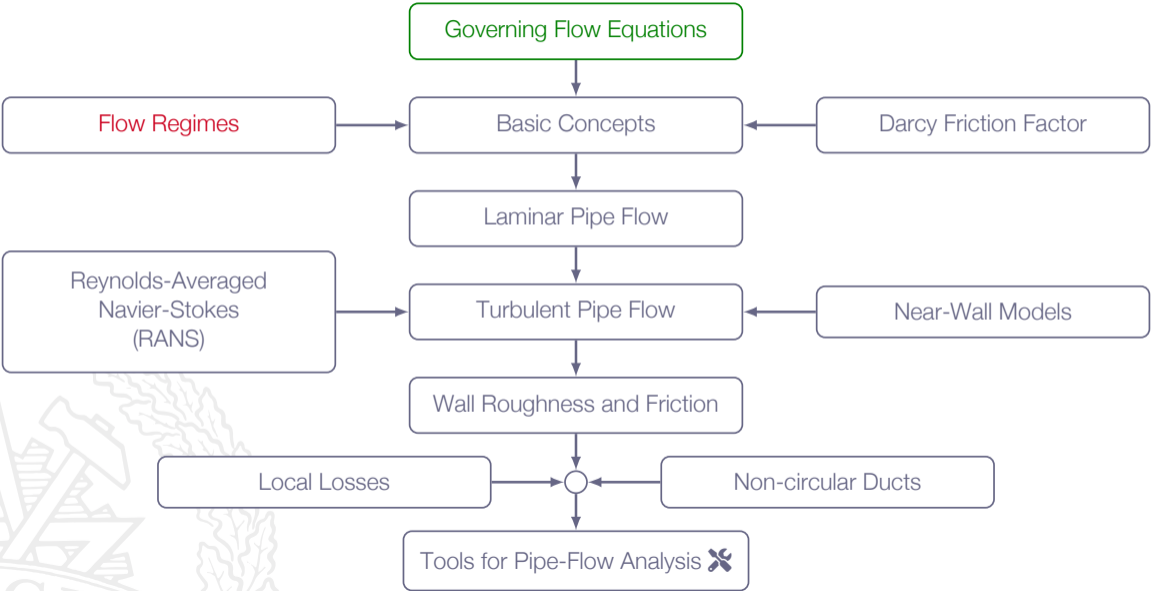
## Example II:

Given the pressure drop available from a pump - what flow rate can be expected

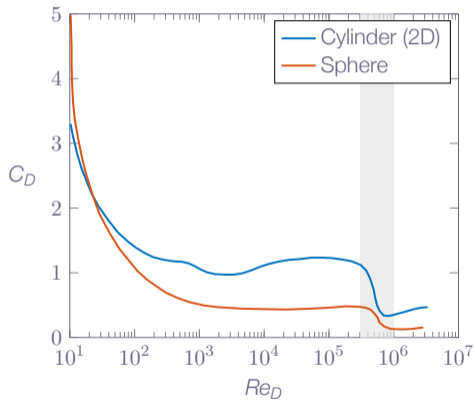
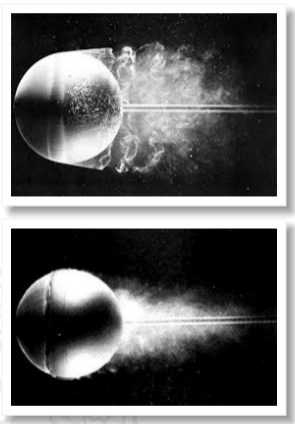




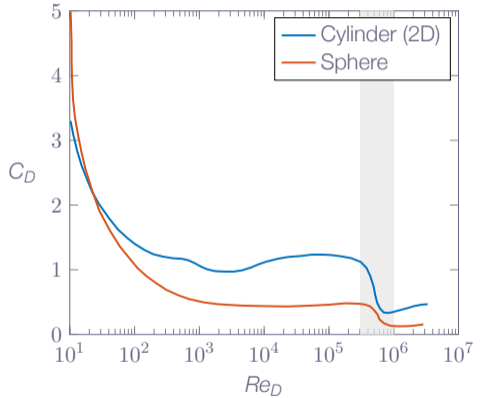
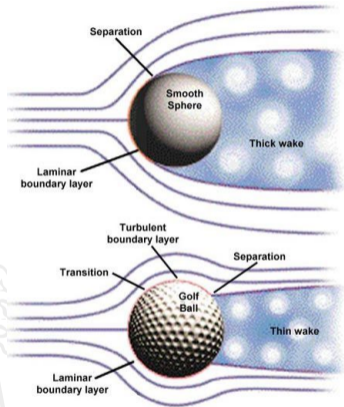
# Roadmap - Viscous Flow in Ducts



# Transition to Turbulence



# Transition to Turbulence



# Transition to Turbulence

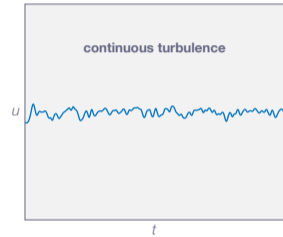
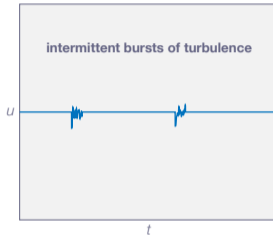
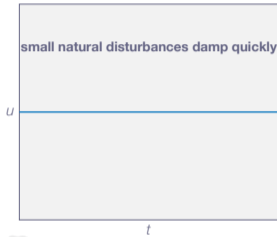
Factors that affects the transition to turbulent flow:

- ▶ Wall roughness
- ▶ Fluctuations in incoming flow
- ▶ Reynolds number



# Transition to Turbulence

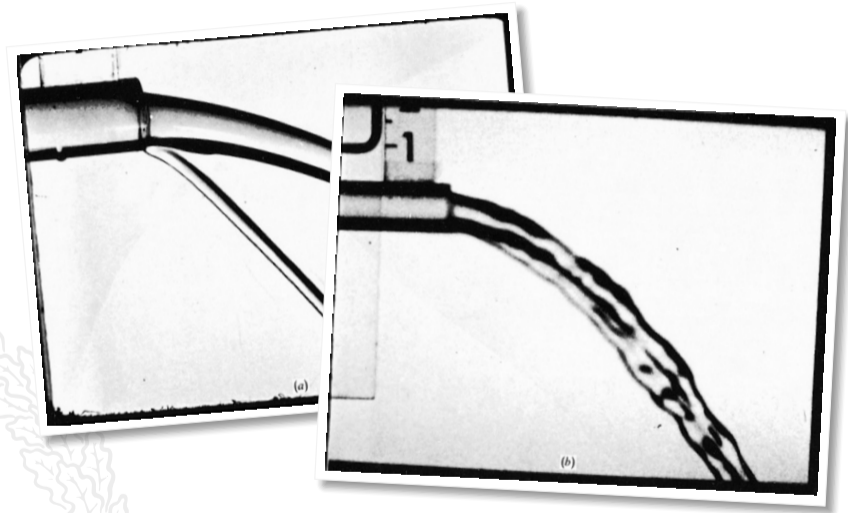
Reynolds number



Fluctuations in the fully turbulent flow velocity signal:

- ▶ typically 1% to 20% of the average velocity
- ▶ not periodic
- ▶ random
- ▶ continuous range (spectrum) of frequencies

# Transition to Turbulence



# Transition to Turbulence - Viscous Flow in Ducts

0	$< Re <$	1	highly viscous laminar "creeping" motion
1	$< Re <$	100	laminar, strong Reynolds number dependence
100	$< Re <$	$10^3$	laminar, boundary layer theory useful
$10^3$	$< Re <$	$10^4$	transition to turbulence
$10^4$	$< Re <$	$10^6$	turbulent, moderate Reynolds number dependence
$10^6$	$< Re <$	$\infty$	turbulent, slight Reynolds number dependence

**Note!** The ranges will vary somewhat with geometry and surface roughness

# Transition to Turbulence - Viscous Flow in Ducts

An accepted design value for **pipe flow transition** is

$$Re_{d,crit} \approx 2300$$

## Note!

1. this value is **for pipe flows**, other applications have different transition Reynolds numbers
2. by careful design the Reynolds number can be pushed to higher values



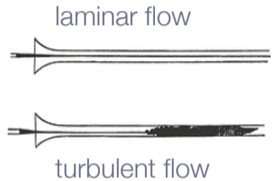
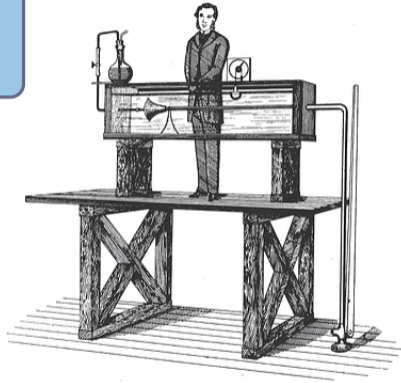
# Transition to Turbulence - Viscous Flow in Ducts

*The great majority of our analyses are concerned with laminar flow or with turbulent flow, and one should not normally design a flow operation in the transition region.*



# Transition to Turbulence - Osborne Reynolds (1842-1912)

$$Re = \frac{\rho U D}{\mu}$$



Re

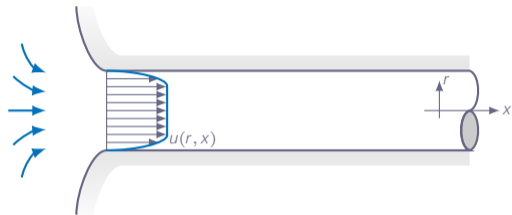


# Internal Flows

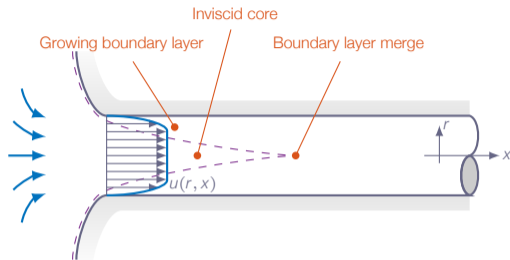
- ▶ **Wall-bounded flows** - constrained by bounding walls
- ▶ Boundary layers grows and meet at the center



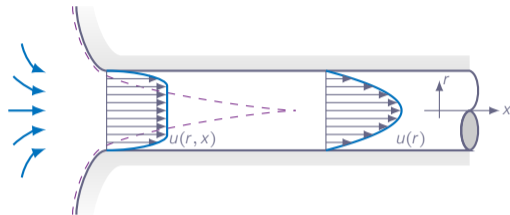
# Velocity Profile Development



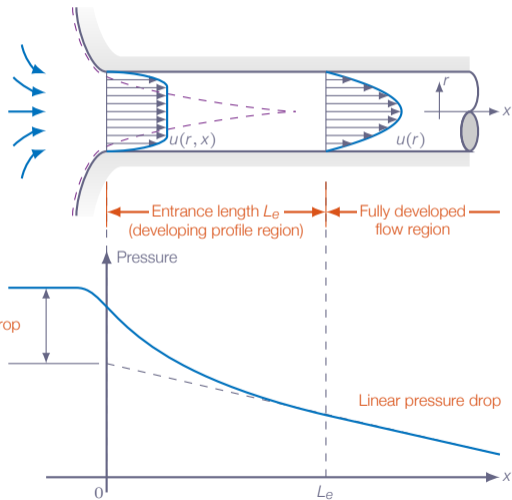
# Velocity Profile Development



# Velocity Profile Development



# Velocity Profile Development



# Velocity Profile Development

$$L_e = f(d, V, \rho, \mu), \quad V = \frac{Q}{A}, \quad Q = \int u dA = \text{const}$$

Dimensional analysis gives:

$$\frac{L_e}{d} = g\left(\frac{\rho V d}{\mu}\right) = g(Re_d)$$





# Velocity Profile Development

Laminar flow:

$$\frac{L_e}{d} \approx 0.06 Re_d$$

The maximum laminar entrance length, at  $Re_d = Re_{d,crit} = 2300$ , is  $L_e = 138d$ , which is the longest development length possible



# Velocity Profile Development

Turbulent flow ( $Re_d \leq 10^7$ ):

$$\frac{L_e}{d} \approx 1.6 Re_d^{1/4}$$

$Re_d$	$4.0 \times 10^3$	$1.0 \times 10^4$	$1.0 \times 10^5$	$1.0 \times 10^6$	$1.0 \times 10^7$
$L_e/d$	13	16	28	51	90